

Properties of Platonic Solids				
Regular Polyhedron	Vertices ( $V$ )	Edges ( $E$ )	Faces ( $F$ )	$V - E + F$
tetrahedron	4	6	4	2
cube	8	12	6	2
octahedron	6	12	8	2
dodecahedron	20	30	12	2
icosahedron	12	30	20	2

### Example 1 Hexagons and Platonic Solids

Why are none of the Platonic solids made with regular hexagons? Explain using angle measures.

#### SOLUTION

Each angle in a regular hexagon measures  $120^\circ$ . At least three hexagons would need to be placed at each vertex.



This means that each vertex would have a total measure of  $120^\circ \times 3 = 360^\circ$ .

But,  $360^\circ$  is the angle of a point on a plane. If the angles added to  $360^\circ$ , the hexagons would make a tessellation, not a polyhedron.

#### Math Language

A **tessellation** is a repeating pattern of polygons that completely covers a plane with no gaps or overlaps.

### Example 2 Angles of Platonic Solids

- a. What is the sum of the measures of the angles at a vertex of a regular octahedron?

#### SOLUTION

Each vertex is the meeting point of four equilateral triangles. The measure of each angle in an equilateral triangle is  $60^\circ$ .

$$60^\circ \times 4 = 240^\circ$$

The sum of the angles is  $240^\circ$ .

- b. What is the sum of the measure of the angles at a vertex of a cube?

#### SOLUTION

Each vertex is the meeting point of three squares. The measure of each angle in a square is  $90^\circ$ .

$$90^\circ \times 3 = 270^\circ$$

The sum of the angles is  $270^\circ$ .

